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# HEATING AND COOLING OPERATIONS OF T-PIPE OF THE USE TRD REGULATIONS

#### 1. Introduction

В статі представлено методику визначення максимальних допустимих швидкостей нагрівання і охолодження, розроблену на основі німецького стандарту TRD 301. Об'єктом досліджень є трійник, виконаний із сталі 13 HMF. У праці приведено геометричний опис трійника, властивості матеріалів, а також характеристику робочих умов. Представлені також отримані значення максимальних допустимих швидкостей нагрівання і охолодження.

The mentioned T-pipe is pressurized element of a power unit. Temperature's changes appear there during starting, load changing and stopping. A non-homogeneous temperature distribution is a cause of thermal stresses. The stresses should not to exceed allowable values thus an identification of allowable heating and cooling rates is so important, particularly for the T-pipe [1-3]. The author presents the calculations of allowable heating and cooling rate conducted according to German TRD 301 regulations [4].

Ключові слова: стандарт TRD 301, трійник, властивості матеріалів.

### 2. Description of the approach and work methodology

#### 2.1. Geometrical properties of the T-pipe and their mean substitutes

The calculation of allowable cooling and heating rates for the T-pipe made from ferritic steel 13HMF (Fig.1) was conducted. The T-pipe is typically utilized in pipelines of a fresh and overheated steam in a power unit of a power plant 360 MW.



Fig.1. Dimensions of T-pipe made from ferritic steel 13HMF

Dimensions of the T-pipe are as following:

-	external diameter of the T-pipe	$d_a = 506 [\text{mm}]$	
-	internal diameter of the T-pipe	$d_i = 290  [\text{mm}]$	
-	thickness of the T-pipe wall	$s_e = 108 [\text{mm}]$	
-	external diameter of the ramification	$d_A = 448 [\text{mm}]$	
-	internal diameter of the ramification	$d_{Ai} = 290  [mm]$	
-	thickness of the ramification wall	$s_A = 79 [\text{mm}]$	
-	ovality	U = 0%	
2.2. Working environment for the T-pipe made from steel 13HMF			
There was assumed that the element works in the following conditions:			
-	minimum pressure in a cycle	$p_{min} = 0 [MPa]$	
-	maximum pressure in a cycle	$p_{max} = 18 \text{ [MPa]}$	
-	minimum temperature in a cycle	$\vartheta_{\min} = 20 [^{\circ}C]$	
-	maximum temperature in a cycle	$\vartheta_{\text{max}} = 540  [^{\circ}\text{C}]$	
-	required start and stopping cycles	n = 2000	

number of cycles (start from cold state 20°C) till cracking appears  $n_{\text{max}} = 5n = 10000$ 

For the considered load cycle a reference temperature  $9^*$  was calculated following the formula:  $\theta^* =$ 

# 2.3. Material properties

Material properties for the steel of 13HMF may be read from strength tables for an assumed temperature, evaluated according to linear interpolation or calculated according to table's factors. The greatest allowable pressure of a working medium is assigned as a working pressure  $p_4$ . For the mentioned element made from the steel 13HMF the following material properties were determined:

- minimum tensile strength at the environment temperature 20 [°C]  $\sigma_{\min B} = 490$  [MPa]
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- \_
- minimum yield strength..... $\sigma_{0.2/9*} = 224$  [MPa]
- linear coefficient of thermal expansion..... $\beta_{L9*} = 1,404 \cdot 10^{-5} [1/K]$
- temperature equalization ratio ..... $\alpha_{9*} = 528 \text{ [mm^2/min]}$

All variables mentioned above dependent on temperature relate to the reference temperature  $\vartheta^*$  for the considered load cycle.

#### 2.4. Stresses calculations

The calculations of stresses were the next stage. The stresses in the T-pipe originated from the working pressure p4 are equal to  $\sigma_{ip4} = 88.5$  [MPa]. The stresses in the element originated from the minimum pressure are equal to  $\sigma_{ip} = 0$  [MPa]. The minimum stresses in the cycle are equal to  $\sigma_{i min} = -214,5$  [MPa]. The maximum stresses in the cycle are equal to  $\sigma_{imax} = 303$  [MPa]. The stresses were calculated with the assumption that stress concentration ratio is equal to  $\dot{a_m} = 3,2$ .

When the maximum and minimum allowable stresses were determined, allowable differences of the temperature were calculated and – at last – allowable heating and cooling rates. For the simplicity, a code-based V factor was introduced:

$$V = \frac{a_{s^*}}{\Phi_{f'} s_b^2} \left[ \frac{1}{\min} \right]$$
<sup>(2)</sup>

where:  $\alpha_{9*}$  - temperature equalization ratio,  $\Phi_f$  - shape factor,  $s_b$  - substituted wall thickness. The shape factor is evaluated from the formula:

$$\Phi_f = \frac{1}{8} \cdot \frac{(u_o^2 - 1) \cdot (3 \cdot u_o^2 - 1) - 4 \cdot u_o \cdot 4 \cdot \ln(u_o)}{(u_o^2 - 1) \cdot (u_o^2 - 1)^2} \qquad \Phi_f = -0,469$$
(3)

where:  $u_0$  – quotient of the external to internal diameters. Then V factor may be evaluated from formula (2) giving:

$$V = -0,073 \left[ \frac{1}{\min} \right] \tag{4}$$

### 3. Achieved results

The allowable heating rate at the beginning of the starting phase is given by the formula:

The allowable heating rate at the end of the starting phase is given by the formula:

$$v_{91} = V \cdot \Delta_{91} \left[ \frac{K}{\min} \right] \qquad \qquad v_{91} = 2,993 \left[ \frac{K}{\min} \right] \tag{6}$$

The allowable cooling rate at the beginning of the stopping phase is given by the formula:

$$v_{92} = V \cdot \Delta_{92} \left[ \frac{\kappa}{\min} \right] \qquad \qquad v_{92} = -2,119 \left[ \frac{\kappa}{\min} \right] \tag{7}$$

The allowable cooling rate at the end of the stopping phase is given by the formula:

$$v_{92} = V \cdot \Delta_{92} \left[ \frac{\kappa}{\min} \right] \qquad \qquad v_{92} = -2,993 \left[ \frac{\kappa}{\min} \right] \tag{7}$$

## 4. Proposed procedure for calculation of heating and cooling rates for any element

Calculations were executed in system Mathcad using formulas from TRD 301 regulations. Presented below is a procedure enabling the calculation, allowable heating and cooling rates for a T-pipe of any geometry or other element working under conditions of high temperature and pressure. The first stage of the calculations is to provide the geometry of the element its theromophisical and strength parameters and conditions under which it will work (fig.4.1).

Технічні науки

🚱 Mathcad Professional - [Tr	ójnik_TRD.mcd]	
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Dimensions:		~
d <sub>a</sub> := 506-mm	external diameter of the T-pipe	
s := 108-mm	thickness of the T-pipe wall	
U := 0	ovality	
Working environment :	minimum pressure in a cycle	
Pmin - 0-MPa	maximum pressure in a cycle	
9	minimum temperature in a cycle	
9 := 540-C	maximum temperature in a cycle	
n := 2000	required start and stopping cycles	
n <sub>max</sub> := 5-n	number of cycles till cracking appears	n <sub>may</sub> = 10000
p <sub>4</sub> := 18·MPa	working pressure	11124
Eq., 1.841-10 <sup>5</sup> -MPa	elastic modulus	
σ <sub>0.29ob1</sub> := 224-MPa	minimum yield strength	
$\beta_{L:9ob1} := 1.404 \cdot 10^{-5} \cdot \frac{1}{K}$	linear coefficient of thermal expansion	
a <sub>Bobl</sub> := 528. mm <sup>2</sup> /min	temperature equalization ratio	
σ <sub>minB</sub> := 490-MPa	minimum tensile strength at the environment tem	perature 20 [oC]
v := 0.3	Poisson's ratio	
Reference temperature:		
ອ <sub>ob1</sub> := 0.75-ອ <sub>max</sub> + 0.25-ອ <sub>min</sub> Analytical dimension	1	9 <sub>001</sub> = 410C
s <sub>b</sub> := 1.15-s	analytical wall thickness	s <sub>b</sub> = 124.2mm
$d_i := d_a - 2 \cdot s_b$	analitycal internal diameter	d <sub>i</sub> = 257.6mm
$d_m := 0.5 \cdot (d_a + d_i)$	average diameter	d <sub>m</sub> = 381.8mm
$u_0 := 1 + 2 \cdot \frac{s_b}{d_i}$		u <sub>o</sub> = 1.964
Press F1 for help.		AUTO NUM Page 2

Fig. 4.1. The geometry, thermo-physical properties and working environment condition – definitions in Mathcad

Keeping determined geometrical parameters, the allowable amplitude of stress changes  $\sigma_a$  is evaluated. If the allowable range of stress changes at the reference temperature  $\sigma_a$  is greater than or equal to doubled minimum yield strength at the reference temperature, it is necessary to calculate reduced allowable range of stress changes (fig. 4.2). The next step are an evaluation of T-pipe stresses induced by pressure (fig. 4.3), minimum stresses in the cycle and maximum stresses in the cycle (fig. 4.4). The factor  $f_u(p)$  – dependent on the ovality – is assumed to be equal to 0 on the cause of the assumption of the ovality U = 0.

Allowable amplitude of stress			^
$S_1 := 78724.99997 + \frac{965775936.9 \cdot K}{(\mathfrak{P}_{obl} - 13137.5 \cdot K)}$		$S_1 = 2.844 \times 10^3$	
$S_2 := 2877.06645 + \frac{4861735.668 \cdot K}{(9_{obl} - 2542.868719 \cdot K)}$		S <sub>2</sub> = 597.631	
$S_3 := 528.0508475 + \frac{261452.4563 \cdot K}{(9_{obl} - 1448.305085 \cdot K)}$		S <sub>3</sub> = 276.244	١
$C_1 := \sqrt{\frac{S_2 - S_3}{S_1 - S_2}} \qquad B := \frac{S_1 - S_2}{\left(C_1\right)^2 \cdot \left[1 - \left(C_1\right)^2\right]}$	$A := S_1 - B \cdot (C_1)^2$	$C_1 = 0.378$	
		$B = 1.832 \times 10^4$ A = 222.585	
$\sigma_{a} := A + B \cdot (n_{max})^{\log(C_{1})}$	+	σ <sub>a</sub> = 597.631	
$\sigma_a := 597.631 \cdot MPa$			~
		>	•
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Fig. 4.2. Calculation of allowable amplitude of stress changes

Stresses from pressure calculations	^
$\alpha_{mo} := 3.2$ theoretical stress concentration factor	$\alpha_{mo} = 3.2$
f <sub>4</sub> := 1.0	f <sub>4</sub> = 1
$\mathbf{f}_{\mathbf{u}}(\mathbf{p}_{4}) := 0$ if $\mathbf{U} = 0$ then $\mathbf{f}_{\mathbf{u}}(\mathbf{p}_{4}) = 0$	$f_u(p_4) = 0$
$\alpha_{\mathbf{m}}(\mathbf{p}_{4}) \coloneqq \alpha_{\mathbf{mo}} \cdot \mathbf{f}_{4} + 2 \cdot \mathbf{f}_{\mathbf{u}}(\mathbf{p}_{4})$	$\alpha_{m}(p_{4}) = 3.2$
$\sigma_{ip4} \coloneqq \alpha_m(p_4) \cdot p_4 \cdot \frac{d_m}{2 \cdot s_b} \qquad \qquad \text{stress from working pressure}$	$\sigma_{ip4} = $ 88.533 MPa
$f_u(p_{max}) := 0$	$f_u(p_{max}) = 0$
$\alpha_{m}(\mathbf{p}_{max}) \coloneqq \alpha_{mo} \cdot \mathbf{f}_{4} + 2 \cdot \mathbf{f}_{u}(\mathbf{p}_{max})$	$\alpha_{\rm m}(p_{\rm max}) = 3.2$
$\sigma_{maxip} := \alpha_m (p_{max}) \cdot p_{max} \cdot \frac{d_m}{2 \cdot s_b}$ stress from maksimum pressure	σ <sub>maxip</sub> = 88.533 MPa
$\mathbf{f_u}(\mathbf{p_{min}}) \coloneqq 0$	$f_u(p_{min}) = 0$
$\alpha_{\mathbf{m}}(\mathbf{p}_{\mathbf{min}}) \coloneqq \alpha_{\mathbf{mo}} \cdot \mathbf{f}_{4} + 2 \cdot \mathbf{f}_{\mathbf{u}}(\mathbf{p}_{\mathbf{min}})$	$\alpha_{\rm m}({\bf p}_{\rm min}) = 3.2$
$\sigma_{\min p} := \alpha_m(p_{\min}) \cdot p_{\min} \cdot \frac{d_m}{2 \cdot s_b}$ stress from minimum pressure	σ <sub>minip</sub> = 0 MPa
	<u>&gt;</u>
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Fig. 4.3. Calculation of stresses induced by pressure



Fig. 4.4. Calculation of maximum and minimum stresses in the cycle

Keeping determined maximum and minimum allowable stresses, the allowable temperature differences is evaluated. The allowable temperature difference (a difference between element internal surface temperature and an average temperature of the wall) is evaluated on the base of formulas for four cases: the beginning of the starting phase, the end of the starting phase, the beginning of the stopping phase, the end of the stopping phase. For the formulas simplicity, the factor W is introduced (fig. 4.5). And finally the allowable heating and cooling rates are determined (fig. 4.6).

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Allowable temperature difference			^
$W := \frac{1 - v}{2 \cdot \beta_{L \vartheta o b l} \cdot E_{\vartheta o b l}}$		$W = 0.135 \frac{K}{MPa}$	
$\Delta \vartheta_1 := W \cdot \left( \sigma_{mini} - \sigma_{minip} \right)$	beginning of the starting phase	$\Delta \vartheta_1 = -29.039 \mathrm{K}$	
$\Delta \boldsymbol{\vartheta}_{1'} \coloneqq \mathbf{W} \cdot \left( \boldsymbol{\sigma}_{mini} - \boldsymbol{\sigma}_{maxip} \right)$	end of the starting phase	$\Delta \vartheta_{1'} = -41.027 \mathrm{K}$	
$\Delta \boldsymbol{\vartheta}_{2} \coloneqq \boldsymbol{W} \cdot \left( \boldsymbol{\sigma}_{maxi} - \boldsymbol{\sigma}_{maxip} \right)$	beginning of the stopping phase	$\Delta \vartheta_2 = 29.039 \mathrm{K}$	
$\Delta \boldsymbol{9}_{2'} \coloneqq \mathbf{W} \cdot \left( \boldsymbol{\sigma}_{maxi} - \boldsymbol{\sigma}_{minip} \right)$	end of the stopping phase	$\Delta \vartheta_{2^{t}} = 41.027 \mathrm{K}$	
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Fig. 4.5. Calculation of allowable temperature differences



Fig. 4.6. Calculation of allowable temperature rates

#### 4. Conclusion

The valid determination of the rates, which power plant pressurized elements may be heated and cooled with, is very important because assuming improper working parameters may lead to lesser durability of elements or their damage. The allowable cooling and heating rates for the T-pipe were calculated basing on TRD 301 regulations [4]. The details of the calculation are presented in this paper. This article presents a procedure enabling the calculation of allowable heating and cooling rates for any pressure element following definition of its dimensions, working parameters and thermophysical properties. This procedure has been suitably verified on such power unit components as: T-piece, main steam valve and drum.

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